## Formula Reference Sheet

<table>
<thead>
<tr>
<th>Shape</th>
<th>Formulas for Area (A) and Circumference (C)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Triangle</td>
<td>$A = \frac{1}{2}bh = \frac{1}{2} \times \text{base} \times \text{height}$</td>
</tr>
<tr>
<td>Rectangle</td>
<td>$A = lw = \text{length} \times \text{width}$</td>
</tr>
<tr>
<td>Trapezoid</td>
<td>$A = \frac{1}{2}(b_1 + b_2)h = \frac{1}{2} \times \text{sum of bases} \times \text{height}$</td>
</tr>
<tr>
<td>Parallelogram</td>
<td>$A = bh = \text{base} \times \text{height}$</td>
</tr>
</tbody>
</table>
| Circle    | $A = \pi r^2 = \pi \times \text{square of radius}$  
            | $C = 2\pi r = 2 \times \pi \times \text{radius}$  
            | $C = \pi d = \pi \times \text{diameter}$ |

<table>
<thead>
<tr>
<th>Figure</th>
<th>Formulas for Volume (V) and Surface Area (SA)</th>
</tr>
</thead>
</table>
| Rectangular Prism | $V = lwh = \text{length} \times \text{width} \times \text{height}$  
                        | $SA = 2lw + 2lw + 2lh$  
                        | $= 2(\text{length} \times \text{width}) + 2(\text{height} \times \text{width}) + 2(\text{length} \times \text{height})$ |
| General Prisms | $V = Bh = \text{area of base} \times \text{height}$  
                        | $SA = \text{sum of the areas of the faces}$ |
| Right Circular Cylinder | $V = Bh = \text{area of base} \times \text{height}$  
                        | $SA = 2B + Ch = (2 \times \text{area of base}) + (\text{circumference} \times \text{height})$ |
| Square Pyramid | $V = \frac{1}{3}Bh = \frac{1}{3} \times \text{area of base} \times \text{height}$  
                        | $SA = B + \frac{1}{2}P\ell$  
                        | $= \text{area of base} + (\frac{1}{2} \times \text{perimeter of base} \times \text{slant height})$ |
| Right Circular Cone | $V = \frac{1}{3}Bh = \frac{1}{3} \times \text{area of base} \times \text{height}$  
                        | $SA = B + \frac{1}{2}C\ell = \text{area of base} + (\frac{1}{2} \times \text{circumference} \times \text{slant height})$ |
| Sphere    | $V = \frac{4}{3}\pi r^3 = \frac{4}{3} \times \pi \times \text{cube of radius}$  
                        | $SA = 4\pi r^2 = 4 \times \pi \times \text{square of radius}$ |
Equations of a Line

Standard Form:
$Ax + By = C$
where $A$ and $B$ are not both zero

Slope-Intercept Form:
$y = mx + b$ or $y = b + mx$
where $m$ = slope and $b$ = y-intercept

Point-Slope Form:
$y - y_1 = m(x - x_1)$
where $m$ = slope, $(x_1, y_1)$ = point on line

Coordinate Geometry Formulas

Let $(x_1, y_1)$ and $(x_2, y_2)$ be two points in the plane.

Slope:
$slope = \frac{y_2 - y_1}{x_2 - x_1}$ where $x_2 \neq x_1$

Midpoint:
$midpoint = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$

Distance:
$distance = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

Distance Traveled

$d = rt$
distance = rate $\times$ time

Simple Interest

$I = prt$
interest = principal $\times$ interest rate $\times$ time

Polygon Angle Formulas

Sum of degree measures of the interior angles of a polygon:
$180(n - 2)$

Degree measure of an interior angle of a regular polygon:
$\frac{180(n - 2)}{n}$
where $n$ is the number of sides of the polygon

Formulas for Right Triangles

Pythagorean Theorem:
$a^2 + b^2 = c^2$

$\sin A = \frac{a}{c} = \left(\frac{\text{opposite}}{\text{hypotenuse}}\right)$

$\cos A = \frac{b}{c} = \left(\frac{\text{adjacent}}{\text{hypotenuse}}\right)$

$\tan A = \frac{a}{b} = \left(\frac{\text{opposite}}{\text{adjacent}}\right)$

Special Triangles

30°-60°-90° Triangle:
- $a$ = shortest side
- $a\sqrt{3}$ = middle side
- $2a$ = longest side

45°-45°-90° Triangle:
- $a\sqrt{2}$ = both legs
- $a$ = hypotenuse

45°-60°-90° Triangle:
- $a\sqrt{3}$ = longest side
- $a$ = shortest side
- $2a$ = middle side
MATHEMATICS BRIEF CONSTRUCTED RESPONSE RUBRIC

3 The response indicates application of a reasonable strategy that leads to a correct solution in the context of the problem. The representations essentially are correct. The explanation and/or justification is logically sound, clearly presented, fully developed, supports the solution, and does not contain significant mathematical errors. The response demonstrates a complete understanding and analysis of the problem.

2 The response indicates application of a reasonable strategy that may be incomplete or undeveloped. It may or may not lead to a correct solution. The representations are fundamentally correct. The explanation and/or justification supports the solution and is plausible, although it may not be well developed or complete. The response demonstrates a conceptual understanding and analysis of the problem.

1 The response indicates little or no attempt to apply a reasonable strategy or applies an inappropriate strategy. It may or may not have the correct answer. The representations are incomplete or missing. The explanation and/or justification reveals serious flaws in reasoning. The explanation and/or justification may be incomplete or missing. The response demonstrates a minimal understanding and analysis of the problem.

0 The response is completely incorrect or irrelevant. There may be no response, or the response may state “I don’t know.”

MATHEMATICS EXTENDED CONSTRUCTED RESPONSE RUBRIC

4 The response indicates application of a reasonable strategy that leads to a correct solution in the context of the problem. The representations are correct. The explanation and/or justification is logically sound, clearly presented, fully developed, supports the solution, and does not contain significant mathematical errors. The response demonstrates a complete understanding and analysis of the problem.

3 The response indicates application of a reasonable strategy that may or may not lead to a correct solution. The representations are essentially correct. The explanation and/or justification is generally well developed, feasible, and supports the solution. The response demonstrates a clear understanding and analysis of the problem.

2 The response indicates application of a reasonable strategy that may be incomplete or undeveloped. It may or may not lead to a correct solution. The representations are fundamentally correct. The explanation and/or justification supports the solution and is plausible, although it may not be well developed or complete. The response demonstrates a conceptual understanding and analysis of the problem.

1 The response indicates little or no application of a reasonable strategy. It may or may not have the correct answer. The representations are incomplete or missing. The explanation and/or justification reveals serious flaws in reasoning. The explanation and/or justification may be incomplete or missing. The response demonstrates a minimal understanding and analysis of the problem.

0 The response is completely incorrect or irrelevant. There may be no response, or the response may state “I don’t know.”

Explanation refers to the student using the language of mathematics to communicate how the student arrived at the solution. Justification refers to the student using mathematical principles to support the reasoning used to solve the problem or to demonstrate that the solution is correct. This could include the appropriate definitions, postulates, and theorems. Essentially correct representations may contain a few minor errors such as missing labels, reversed axes, or scales that are not uniform. Fundamentally correct representations may contain several minor errors such as missing labels, reversed axes, or scales that are not uniform.
CUES FOR STUDENTS

Analysis

• Consider what the question asks you to do.
  1. What information is given in the problem?
  2. What information do you need to solve the problem?
• Think about what you would do to solve the problem.

* Representation

• Define the variables.
  Let \( x = \ldots \) and/or let \( y = \ldots \).
• Create a graph, chart, or table.
  Include titles, axes, labels, and scales.
• Create a drawing or construction.
  ✦ Construction: For the high school assessment, students may use a compass, a straightedge, patty paper, a Mira™, and/or a mirror for an item requiring a construction. Measurement cannot be part of the strategy.
  ✦ Drawing: Students may use a compass, a ruler, patty paper, a Mira™, a mirror, and/or a protractor for an item requiring a drawing. Measurement can be part of the strategy.

Application

• Solve the problem.
• Write the answers in the context of the problem.
• Be sure you answer what is asked for in the problem.
• Check to see if the answer is reasonable.

* Explanation

• Write or describe the steps you used to solve the problem.

* Justification

• Use mathematics (definitions, theorems, reasoning, principles) to support your solution and/or process.
  1. Write the mathematics concepts you used.
  2. Tell why you solved the problem as you did.
  3. Demonstrate that the solution is correct.

* Complete as appropriate and required by the problem.